

$$\min_{\Theta, p} J(\Theta, p) = \sum_i \lambda_i J_i(\Theta, p)$$

**Optimal control**

$$\Theta = \begin{bmatrix} \mathbf{u}_0 \\ \mathbf{u}_1 \\ \vdots \\ \mathbf{u}_p \end{bmatrix}$$

$$J_{ene}(\Theta, p) = \|M\Theta\|^2$$

$$J_{acc}(\Theta, p) = \|\mathbf{y}_p - \hat{\mathbf{y}}_p\|^2 \quad \hat{\mathbf{y}}_p = \begin{bmatrix} \hat{r}_x \\ \hat{r}_y \\ \hat{r}_z \end{bmatrix}$$

$$J_{dur}(\Theta, p) = \left(1 - \frac{1}{1+\beta p}\right) = J_{dur}(p)$$

### Listing's law for saccades: I

- minimal duration (single-axis rotation)
- minimal total energy ( $\propto (\text{control vel.})^2$ )
- accuracy cost ( $r_x=0$  at end)

$$J_{acc}(\Theta, p) = \|\mathbf{y}_p - \hat{\mathbf{y}}_p\|^2 \quad \hat{\mathbf{y}}_p = \begin{bmatrix} \hat{r}_y \\ \hat{r}_z \end{bmatrix}$$

$$J_{dur}(\Theta, p) \text{ and } J_{ene}(\Theta, p)$$

$$J_{eff}(\Theta, p) = \mathbf{y}_p^T \mathbf{Q}_f \mathbf{y}_p$$

$Q_f$  = force exerted

### Listing's law for saccades: II

- minimal duration and energy
- accuracy cost (no constraint on  $r_x$ !)
- minimal effort (total summed forces)

